## Definitions

amortisation: The paying off of a loan in regular instalments over a period of time.
annuity: An investment that has regular and constant payments over a period of time.
annuity investment: An investment that has regular deposits made over a period of time, resulting in the growth of the principal amount.
depreciation: The estimated loss in value of assets as a result of factors including wear and tear, advances in technology, or a lack of demand for those specific items.
effective (annual) interest rate: A rate used to compare the annual interest between loans with different compounding periods, such as daily, weekly or monthly: $r_{\text {eff }}=\left[\left(1+\frac{r}{100 \cdot n}\right)^{n}-1\right] \times 100 \%$
effective life: The length of time that an asset is useful to a business.
flat rate loans: A loan that charges 'flat rate interest' (see simple interest).
future value: The future value of an asset based on the original cost less depreciation.
interest only loans: A loan where the borrower makes only the minimum repayment equal to the interest charged on the loan.
perpetuity: An annuity where a permanently invested sum of money provides regular payments which continue indefinitely.
scrap value: The amount at which an asset is removed from the books of a company as it is considered effectively worthless. Also called the 'write-off value'.
simple interest: Interest calculation based on the original amount borrowed or invested. It is a constant amount; also known as 'flat rate interest'.
superannuation: A fund into which money is contributed by working Australian's employers, and optionally topped up by the employee, each pay period, for use in retirement.
reducing balance depreciation: A method of depreciation where the value of an asset is reduced by a fixed percentage of its previous value. This is an application of compound interest; sometimes called 'diminishing value depreciation'.
reducing balance loans: A loan in which interest is usually charged every month by the financial institution and repayments are made by the borrower on a regular basis. These repayments are larger than the interest for that time period, hence the amount still owing is reduced each time.
unit cost method: A method of depreciating an asset according to its use; the more it is used the faster it will depreciate: $V_{n}=V_{0}-n d$

## Formulas

Recursive formulas - used to find the next term given the current term starting from the initial term $V_{0}$

| Increasing progression (growth) | Decreasing progression (decay) |
| :---: | :---: |
| Simple interest $V_{n+1}=V_{n}+d$ <br> where $d=\frac{V_{0} \cdot r}{100}$ | Flat rate depreciation $V_{n+1}=V_{n}-d$ <br> where $d=\frac{V_{0} \cdot r}{100}$ |
| Compound interest $V_{n+1}=V_{n} \cdot R$ <br> where $R=\left(1+\frac{r}{100}\right)^{2}$ | Reducing balance depreciation <br> where $R=\left(1-\frac{r}{100}\right)$ $V_{n+1}=V_{n} \cdot R$ |
| Annuity investments $V_{n+1}=V_{n} \cdot R+d$ <br> where $R=\left(1+\frac{r}{100}\right)^{r_{n+1}}$ and $d$ is the regular payment | Reducing balance loans $V_{n+1}=V_{n} \cdot R-d$ <br> where $R=\left(1+\frac{r}{100}\right)$ and $d$ is the regular payment |

General formulas - used to find any term given the initial term

| Increasing progression (growth) | Decreasing progression (decay) |
| :---: | :---: |
| Simple interest $V_{n}=V_{0}+d \cdot n$ <br> where $d=\frac{V_{0} \cdot r}{100}$ | Flat rate depreciation $V_{n}=V_{0}-d \cdot n$ <br> where $d=\frac{V_{0} \cdot r}{100}$ |
| Compound interest <br> where $R=\left(1+\frac{r}{100}\right)$ $V_{n}=V_{0} \cdot R^{n}$ | Reducing balance depreciation $V_{n}=V_{0} \cdot R^{n}$ <br> where $R=\left(1-\frac{r}{100}\right)$ |
| Annuity investments $V_{n}=V_{0} \cdot R^{n}+\frac{d \cdot\left(R^{n}-1\right)}{R-1}$ <br> where $R=\left(1+\frac{r}{100}\right)$ and $d$ is the regular payment | Reducing balance loans $V_{n}=V_{0} \cdot R^{n}-\frac{d \cdot\left(R^{n}-1\right)}{R-1}$ <br> where $R=\left(1+\frac{r}{100}\right)$ and $d$ is the regular payment |

Key:

| Symbol | Recursive definition | Application to financial modeling |
| :---: | :---: | :---: |
| $V_{n}$ | the current $V$ | value (price) at $n$ |
| $V_{n+1}$ | the next $V$ | value (price) at $n+1$ |
| $V_{0}$ | the initial $V$ | original amount <br> - principal amount <br> - borrowed amount |
| $d$ | common difference | regular increase/decrease <br> - regular payment amount <br> - unit cost depreciation |
| $R$ | common ratio | compounding factor <br> - $\left(1+\frac{r}{100}\right)$ or $\left(1-\frac{r}{100}\right)$ <br> where $r$ is the nominal interest rate |

